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Turbo Equalization Techniques Toward Robust PDM 16-QAM Optical Fiber Transmission

Valeria Arlunno, Antonio Caballero, Robert Borkowski, Silvia Saldaña Cercós, Darko Zibar, Knud J. Larsen, and Idelfonso Tafur Monroy

Abstract—In this paper, we show numerically and experimentally that turbo equalization (TE) is an efficient technique to mitigate performance degradations stemming from optical fiber propagation effects in both optical fiber dispersion managed and unmanaged coherent detection links. The effectiveness of the proposed solution can be appreciated in both linear and nonlinear regimes for either scenario. We report on a system employing a polarization division multiplexing (PDM) 16-quadrature amplitude modulation (QAM) format for which we accomplish an increment in tolerance to link input power of up to 3 dB that represents a substantial improvement margin. The best bit error rate (BER) performances will therefore be guaranteed in a larger window, 6 dB, of link input power thanks to the implemented TE scheme. Moreover, our proposed approach is also proven to effectively mitigate interchannel impairments from surrounding amplitude shift-keying interfering channels in a dispersion managed link achieving also in this case an increment in power tolerance of 3 dB. Furthermore, in terms of BER performances, our proposed TE approach guarantees a gain of about a half order of magnitude at the best operational point. As TE can be included in the current coherent detection transceiver technologies and complement other equalization techniques, it has prospects for application in next-generation high-capacity and long-reach optical transmission links.

Index Terms—Coherent detection; Convolutional codes; Equalizers; Optical transmission; Signal processing algorithms; Turbo equalization.

I. INTRODUCTION

Higher-order modulation formats constitute an attractive solution toward capacity upgrade of the existing optical fiber infrastructure by exploiting their important feature of high spectral efficiency [1–5]. For example, polarization division multiplexing (PDM) 16-quadrature amplitude modulation (QAM) is considered as a promising candidate for doubling the bit rate per channel with respect to PDM quadrature phase-shift keying (QPSK). In these transmission systems, linear fiber channel impairments, such as chromatic dispersion, group velocity dispersion,

and polarization mode dispersion (PMD), can be effectively mitigated using digital linear signal processing techniques, as has been demonstrated for both QPSK and higher-order QAM signaling [6]. However, transmitter and receiver imperfections, not entirely mitigated by linear techniques, still need to be addressed. Linear processing algorithms are shown to be less effective for compensation of performance impairments stemming from optical fiber nonlinearities, such as self-phase modulation, four-wave mixing, cross-phase modulation, and laser phase noise. Additionally, in mixed modulation format transmission links, nonlinear impairments induced by coexisting 10 Gb/s amplitude shift-keying (ASK) channels introduce a serious degradation to the overall system performance [7]. Moreover, when long transmission reach is targeted, higher power levels launched into the fiber might be required to guarantee extended reach; however, such high optical power level fiber transmission conditions enhance the generation of nonlinear optical fiber impairments.

Several techniques have been reported in the literature to mitigate for nonlinear optical fiber impairments, such as digital backpropagation, maximum likelihood sequence estimation (MLSE), use of radio frequency pilot, pre- and post-compensation, or expectation maximization [8–14]. However, these methods suffer from complexity and depend on particular optical fiber transmission scenarios. Therefore there is a need for efficient equalization techniques to enhance the benefit of the aforementioned nonlinear techniques or to allow us to search for a new lower-complexity solution.

In this paper, we present a scheme based on turbo equalization (TE) equally effective in mitigating accumulated noise induced by link amplification and the effects induced by fiber nonlinearities. We realize a digital signal processing (DSP) structure based on convolutional code (CC), normalized least mean square (NLMS) equalization, and a soft-input soft-output (SISO) routine. TE routines have been proposed for direct detection optical communication systems in order to mitigate the effects of PMD [15,16]. In coherent detection optical fiber communications, until now, experimental demonstration of low-density parity-check (LDPC) coded TE [17–19] has been presented for polarization multiplexed binary phase-shift keying (BPSK) and QPSK. More recently LDPC-coded TE has also been

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evaluated in electrical generated PDM orthogonal frequency division multiplexing (OFDM) 16-QAM for trans-oceanic transmission with large-core/ultra-low-loss fiber [20]. Even though LDPC codes can be very powerful, their implementation remains a challenge due to the complex structure of the decoder, and alternative works are looking for simplified low-complexity solutions [21].

We expand the state of the art by introducing TE for coherent optical links using an advanced modulation format, 16-QAM, including the transmission scenario with unmanaged and managed optical links with standard single-mode fiber (SSMF) and also in the presence of legacy channels in a 100 GHz spectral grid. We perform experimental and numerical validation of the performance of our proposed TE for different fiber transmission lengths. We evaluate the performance both in the linear regime, where the performance is mostly degraded by chromatic dispersion and amplified spontaneous emission (ASE) noise introduced by the amplifier of the transmission link, and in the nonlinear regime, where nonlinearities are the dominant effects of performance degradation. Nevertheless further investigations should be realized to better evaluate the proposed scheme when specific nonlinear effects are targeted. Our TE approach features low complexity stemming from the use of a CC, and its ability to accomplish for each new decoding iteration a more accurate channel estimation. Concatenated Reed–Solomon (RS), Bose–Chaudhuri–Hocquenghem (BCH), and LDPC codes are employed as error correcting schemes in current optical communication products. In our case the employment of a simple and weaker code, i.e., CC, has been chosen to show the advantages of the TE routine and to avoid complexity challenges that solutions based on the other codes would present.

All the presented results in this paper have been obtained employing a PMD 16-QAM coherent detection system. We first implement a TE scheme in a simulation tool, and then we perform experimental validation. For completeness of results we study the effectiveness of our approach in a dispersion uncompensated link, through numerical investigations, and in a dispersion compensated link, through experimental investigations. Both experiment and simulation show that an increment in power tolerance up to 3 dB and a bit error rate (BER) gain of a half order of magnitude can be accomplished, confirming the efficiency of our approach for both scenarios. Additionally we perform experimental validation for PDM 16-QAM transmission surrounded by neighbor 10 Gb/s ASK channels in a 100 GHz spectral grid, a situation in which the transmission reach is severely distorted by cross nonlinear impairments due to the interactions with the copropagating ASK channels. A total increment in power tolerance of up to 3 dB is also accomplished in this case. Both CC and the equalizer contribute in the TE routine to achieve the obtained improvements.

II. TURBO EQUALIZATION

Inspired by turbo codes, TE was first introduced to combat intersymbol interference effects in digital communication systems [22]. A TE system consists of an iterative joint

equalization and decoding technique that can achieve impressive performance gains in terms of signal-to-noise ratio (SNR) for communication systems.

Figure 1 shows the pre-encoder and receiver structure for TE employed in this work. Random generated data 1000 bits long are created with offline processing and encoded by a CC with rate $R = 1/2$ and 16 states trellis. The 2000 coded bits are then interleaved to suppress burst errors and sent to the optical modulator at the transmitter in the physical layer. CCs have up to now only been incompletely explored for optical communications. The drawback of such codes in optical transmission is their high coding overhead compared to high-rate block codes, such as RS codes and LDPC codes. On the other hand, CC codes present attractive features such as simple and straightforward encoding and hard and soft decision decoding algorithms. The large overhead can be alleviated by using CC codes together with bandwidth-efficient modulation. Similar performance to RS codes has been obtained, with the benefit of simpler encoding electronics [23]. In this work we present a simple CC not only for the features presented, but also for convenience purposes in demonstrating its benefits and the advantages of TE. However, a more complex code can be designed and evaluated in the future.

On the receiver side, the received signal after optical transmission and detection is then processed offline. After a 16-QAM DSP receiver [12], the received data are fed into a SISO TE structure. A NLMS adaptive equalizer is applied due to the unknown nature of the transmission channel. We optimize the number of taps and the step to obtain the best performance. Soft information on all the coded bits in the form of log-likelihood ratios (LLRs) is provided by the demapper. A nongray 16-QAM mapping results due to the typical setup configuration on optical systems based on independent binary electronics, requiring a specific

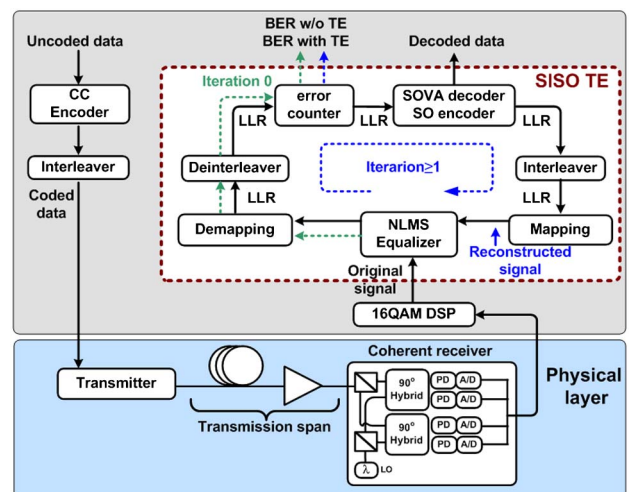


Fig. 1. Pre-encoding and receiver structure of the SISO turbo equalizer algorithm. CC, convolutional code; LO, local oscillator; PD, photodiode; A/D, analog-to-digital converter; DSP, digital signal processing; NLMS, normalized least mean square; LLR, log-likelihood ratio; SOVA, soft-output Viterbi algorithm; SO, soft output; SISO, soft-input soft-output; TE, turbo equalization.

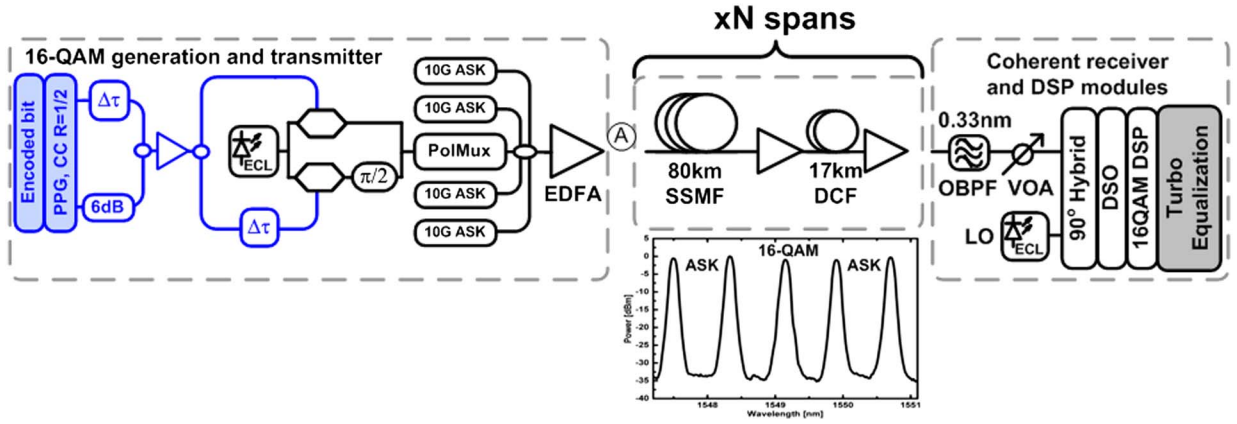


Fig. 3. Experiment setup. PPG, pulse pattern generator; CC, convolutional code; ECL, external cavity laser; EDFA, erbium-doped fiber amplifier; A, launch power measurement point; OBPF, optical bandpass filter; VOA, variable optical attenuator.

amplified, and split into two branches to be fed to an I/Q optical modulator. An external cavity laser (ECL) with a linewidth of 100 kHz is employed at the transmitter. The optical 16-QAM signal is then sent to a polarization multiplexing stage to generate the PDM 16-QAM signals. The experimental evaluations are reported for a baud rate of 10 Gbaud and a bit rate of 80 Gb/s. Four 10 G transponders are then multiplexed with the 16-QAM signal to emulate the interfering channels, which have been placed symmetrically around the central signal with a spacing of 100 GHz. The spectrum of the signal with the neighboring four legacy ASK channels is presented as an inset of Fig. 3. In the center is placed the PDM 16-QAM encoded signal, surrounded by two ASK channels on both sides in a 100 GHz spacing grid. An EDFA is used to adjust the launch power to the link, including a precompensation of the dispersion equivalent to 40 km of SSMF. The transmission link block consists of spans of SSMF of 80 km length and dispersion compensated fiber (DCF) of 17 km length. EDFA amplification is used for span loss compensation. Three link lengths 240, 400, and 640 km, corresponding to a number of spans equal to 3, 5, and 8, respectively, are evaluated. The input power to the link, measured at point A, is varied between -4 and 4 dBm with a granularity of 1 dB. At the receiver side, we apply coherent detection and DSP modules. We employ an ECL with 100 kHz linewidth as the LO and a variable optical attenuator at the signal input to maintain a constant ratio between the signal received and the LO. A 40 GSa/s sampling rate digital signal oscilloscope (DSO) with 13 GHz bandwidth is employed to sample the received signals, and then offline signal processing is performed. The PDM 16-QAM DSP-based receiver earlier presented for the numerical validation case, with exception of the CD compensation module not present for the compensated link, is then applied followed by the SISO TE structure presented above.

C. Metodology

The measured curve for the BER as a function of the link input power, presented in Figs. 3, 5, 6, and 7, and the measured curve for the BER as a function of the lasers'

linewidth, presented in Fig. 4, show results without (w/o) TE and with TE. The first case, when no TE is employed, corresponds to "iteration 0." After demodulating the signal, we apply the hard decision to obtain the stream of bits that forms the received signal. This stream is then directly compared to the one used at the transmitter side in the BER counter block. When TE is applied, we employ the SISO TE structure, using therefore the LLR information of the received signals and making a full iteration. We will then exit the loop at the BER counter stage, as shown in Fig. 1, before starting a new iteration. In both cases, iteration 0 and iteration 1, the error counter is placed before the soft decoder; therefore the results reflect the performance of the original bits, w/o TE, and of the reconstructed bits, with TE, and not the performance of the CC. This also means that the results reported all have the same line rate, and baud rate, chosen at the transmission side, while the decoded results, not reported in this work, would show better performances but with a net rate equal to half the line rate, due to the rate chosen for the CC.

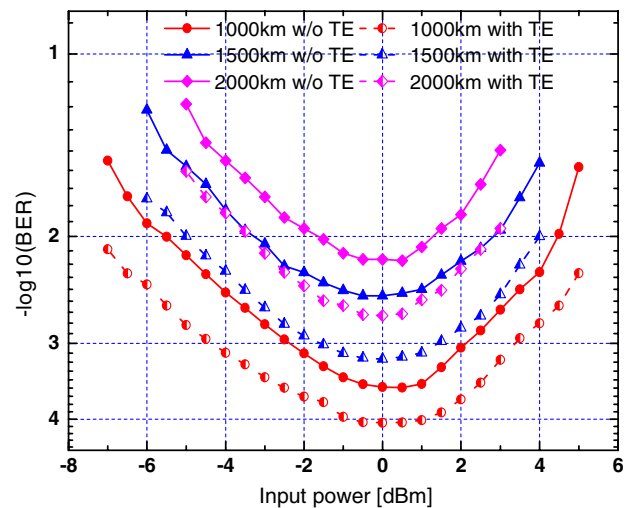


Fig. 4. BER as a function of link input power to the transmission span with and without TE for 1000, 1500, and 2000 km uncompensated SSMF transmission.

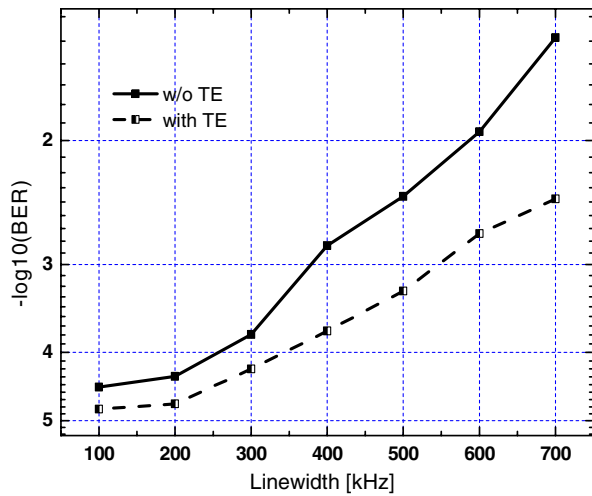


Fig. 5. BER as a function of transmitter and local oscillator laser linewidth for back-to-back with a fixed OSNR value of 25 dB.

For the numerical evaluation of the PDM 16-QAM signal we have created three different realizations, while for the experimental results we have evaluated three different traces of the transmitted signal. That holds for all the results presented and for all the transmission distances considered. In all of them, for both polarizations and for all four bits that constitute the 16-QAM signal, 52 frames of the encoded original data were retrieved. This gives an amount of processed data equal to $\sim 2.5 \times 10^6$ bits, which guarantees sufficient bits for error count of the BER values reported for both numerical and experimental results.

IV. PERFORMANCES OVER UNCOMPENSATED LINK

We first evaluate the performance for the dispersion uncompensated link scenario, through numerical investigations. We study the effectiveness of our approach for

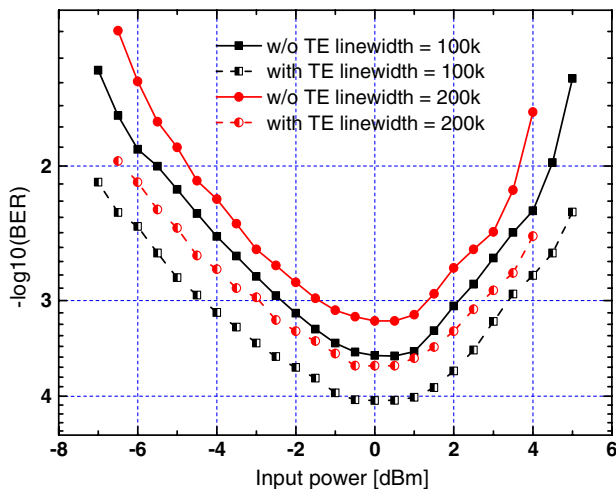


Fig. 6. BER as a function of link input power to the transmission span with and without TE for 100 and 200 kHz linewidth for 1000 km uncompensated SSMF transmission.

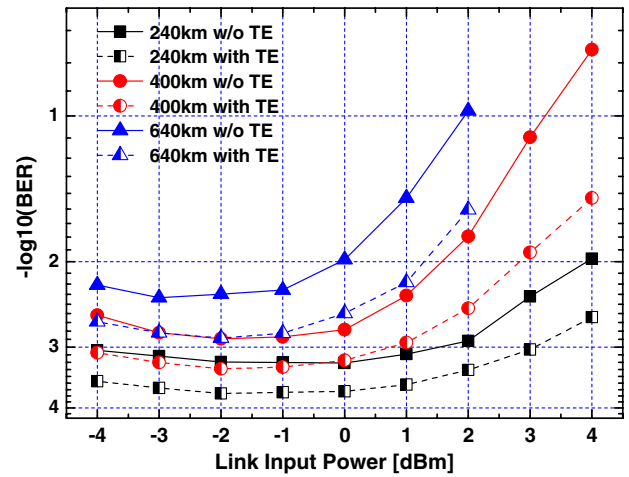


Fig. 7. Performance of single channel. BER as a function of link input power to the transmission span with and without TE for 240, 400, and 640 km compensated link.

different transmission lengths. We then demonstrate that similar performance obtained can be expected with a more commercial laser with higher laser linewidth through numerical investigations of back-to-back and 1000 km total link length scenario.

We consider a transmission link consisting of spans of SSMF of 100 km length. The 16-QAM DSP modules block includes CD compensation, polarization demultiplexing, frequency, and carrier recovery. For the case in which TE is not used, the so-called iteration 0, hard decision BER evaluation is applied. For the case when TE is used, the SISO TE structure explained above is employed after demodulation. We employ a NLMS adaptive equalizer; the number of taps and step size is kept constant throughout all the numerical investigations. A SOVA, based on the soft information provided by the LLR and with 64 states, is used as the decoder. The results of the BER performances as a function of link input power for three different distances are shown in Fig. 4. A total link reach of 1000, 1500, and 2000 km, corresponding to a number of spans of 10, 15, and 20, respectively, has been investigated. We can evaluate the results both on link input power accomplished tolerance and on BER performance gain. It is observed from Fig. 4 that by employing the TE, we accomplish an increment in tolerance to link input power of up to 2 dB. If we consider as an example the case of 1000 km transmission, the best operational point is obtained for a link input power equal to 0 dBm. The same BER performance can be obtained for a link input power to 2 dBm when the TE routine is applied, resulting in the mentioned total increment in tolerance of 2 dB. The same BER performance can be obtained for -2 dBm, and therefore the best operational point BER performance can now be obtained over a window of link input power of 4 dB, from -2 to 2 dBm. In terms of BER performance, our proposed TE approach guarantees a gain of about a half order of magnitude at the best operational point. It should also be noted that this algorithm can extend the maximum total length by 500 km, which corresponds to five spans. We can notice that the results

obtained employing the TE scheme in a 2000 km link outperform the results of a 1500 km length link when no TE is applied.

We then demonstrate that the performances obtained are not related to the laser linewidth value. First we evaluate a back-to-back case, no transmission, and we vary the value of the linewidth parameter of both the transmitter and the LO laser from 100 to 700 kHz with a granularity of 100 kHz. In Fig. 5, we numerically evaluate the BER performances as a function of the value for laser linewidth for a fixed optical signal-to-noise ratio (OSNR) of 25 dB. The results obtained show that our TE routine has similar behavior for all the laser linewidth values considered and can therefore be implemented with commercial distributed feedback lasers. It should also be noted that the TE routine is more effective in the low-performance region, from 400 to 700 kHz, where an improvement of almost one order of magnitude can be seen.

Next we demonstrate the independence from the laser linewidth also in the transmission scenario. We consider uncompensated link transmission with 1000 km of total distance length, and we vary the value of the linewidth parameter of both the transmitter and LO lasers from 100 to 200 kHz. The results are shown in Fig. 6. In this case it is observed that by employing the TE, we accomplish an increment in tolerance to link input power of up to 2 dB, and the best operational point BER performance can now be obtained over a window of link input power of 4 dB. Figure 6 also shows that by employing the TE routine, the results obtained with a linewidth value of 200 kHz outperform the ones with 100 kHz when no TE has been applied. This means that the use of our proposed solution can relax the requirements in terms of laser linewidth value for the transmitter and receiver.

V. EXPERIMENTAL RESULT FOR COMPENSATED OPTICAL FIBER TRANSMISSION LINK

We evaluate the dispersion compensated link scenario through experimental investigations. We study the effectiveness of our approach for different transmission lengths; we then evaluate its effects in the presence of copropagating interfering ASK channels.

We consider a dispersion managed transmission link consisting of spans of SSMF of 80 km length. The dispersion effect is compensated optically by 17 km of DCF. The 16-QAM DSP modules block includes polarization multiplexing, frequency, and carrier recovery. For the case in which TE is not used, the so-called iteration 0, hard decision BER evaluation is applied. For the case in which TE is used, the SISO TE structure explained above is employed after demodulation. We employ a NLMS adaptive equalizer; we optimize the number of taps and the step for all the realizations. A SOVA, based on the soft information provided by the LLR and with 64 states, is used as the decoder.

A. Performances of Single Channel Transmission

First, we evaluate the BER performances obtained through experimental investigations for a single channel transmission scenario. In Fig. 7 the BER performance is plotted as a function of the link input power. We evaluate three link transmission lengths: 240, 400, and 640 km, corresponding to 3, 5, and 8 spans, respectively. We vary the value of the link input power from -4 to +4 dBm with a granularity of 1 dBm. We then evaluate the results both on link input power accomplished tolerance and on BER performance gain. It is observed that by employing the TE, we accomplish an increment in tolerance to link input power of up to 3 dB, and the best operational point BER performance can now be obtained over a window of link input power of 6 dB. The use of the CC can provide a maximum improvement of ~5 dB in the loop, which is seen in the following way. A performance of 10^{-3} after the soft encoder corresponds to ~6 dB of SNR. Before the soft encoder we have a BER of $(1/7) \times 10^{-3}$ (since the generator has 7 ones) corresponding to an E_b/N_0 of ~4 dB. To obtain the aforementioned BER, ~1 dB in entrance to the SOVA block is required. Thus a maximum gain of ~5 dB is provided by the presence of the CC in the loop. The 6 dB increment in the launch power window is therefore provided by the use of the complete TE scheme. In terms of BER performances our proposed TE approach also guarantees a gain of about a half order of magnitude at the best operational point. It should also be noted that the results obtained using the TE routine for 400 and 640 km have similar performances to the results obtained with 240 and 400 km, respectively, when no TE has been applied. For all the transmission lengths, we observe that larger improvement in terms of BER is achieved when the original performances are worse, in this case between 2 and 4 dBm of link input power, where the performance degradation is also dominated by nonlinear effects.

B. Performances With Interfering Channels

In Fig. 8, the BER performance as a function of the link input power is plotted for a multichannel transmission scenario employing PDM 16-QAM and 10 Gb/s ASK surrounding channels in a 100 GHz grid. The 16-QAM signal is placed in the center, while the four interfering channels are placed two on each side. The spectrum is reported as an inset of the experimental setup in Fig. 3. As for the single channel transmission scenario we evaluate three link transmission lengths, 240, 400, and 640 km, and we vary the value of the link input power from -4 to +4 dBm with a granularity of 1 dBm. It is observed that also in this case by employing the TE, we accomplish an increment in tolerance to link input power of up to 3 dB, and the best operational point BER performance can now be obtained over a window of link input power of 6 dB. In terms of BER performances, our proposed TE approach guarantees a gain of about a half order of magnitude at the best operational point. It should also be noted that the results obtained using the TE routine for

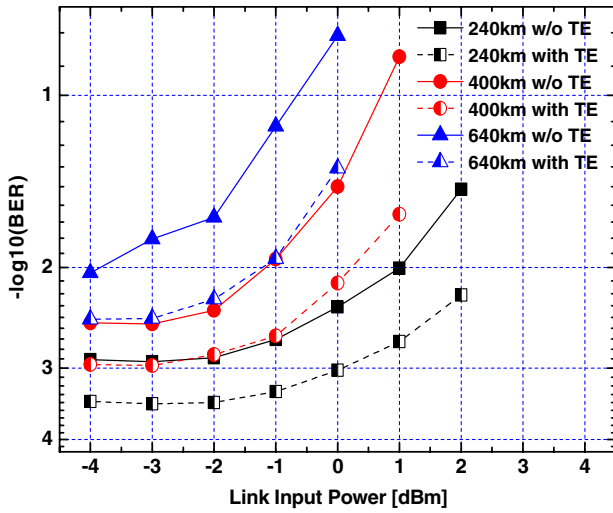


Fig. 8. Performance with interfering OOK channels. BER as a function of link input power to the transmission span with and without TE for 240, 400, and 640 km compensated link.

400 and 640 km show performance similar to the results obtained with 240 and 400 km, respectively, when no TE has been applied. For all the transmission lengths, we observe that larger improvement in terms of BER is achieved for higher link input power, between 2 and 4 dBm, which is the region where the performance degradation is strongly dominated by nonlinear effects. If we consider, for example, 400 km transmission at +1 dBm link input power, we achieve an improvement of almost one order of magnitude in terms of BER performance.

Comparing this result with the single channel reported above, we notice that the total performance is affected by the presence of the ASK interfering channels, which cause a penalty of 3 dB in terms of input power. As an example, it can be pointed out that similar performance for 240 km and 3 dB of input power obtained with a single channel is now reported for the same distance with 0 dB of input power in the presence of ASK interfering channels.

VI. COMPARISON

The BER performance has been evaluated for three different situations: uncompensated link transmission,

through numerical simulations, and compensated link transmission, through experimental investigations, for both single and multichannel scenarios. The performances reported in Figs. 4, 7, and 8 have been obtained for the same sets of link input powers, from -4 to +4 dBm with a granularity of 1 dBm. Therefore we can compare the above-mentioned results in terms of gain system tolerance, which are reported in Table I. Power tolerance, in Table I, represents the accomplished tolerance to link input power obtained through the TE routine. From Table I, we observe that a 2 dB power increment in tolerance is guaranteed for all the numerical evaluations with an unmanaged transmission link. A maximum increment of 3 dB is obtained for the 1500 km transmission case. In the case of the dispersion managed link, investigated through experimental validation, we have evaluated single channel and multichannel transmission with interfering ASK channels, reported as 100 GHz in Table I. For both of these cases and for all the transmission link lengths considered, TE results in a reported increment in power tolerance of 3 dB. Similar to what we obtain for numerical validations, link transmission distances longer than the ones considered in this experimental validation should result in smaller increments. The column labeled “window” represents the sets of link input power for which the best operational point BER performance can be obtained. From Figs. 7 and 8 we can analyze only the right half of the tolerance, 3 dB in all cases, but the results should present the same properties as the numerical investigations, in which case the tolerance on the left side was equal to that on the right side. Δ BER represents the gain in terms of BER obtained by applying TE for the best operational values. We notice that an improvement of about a half order of magnitude has been obtained for numerical investigation. If we consider 1500 km, at the best operational point the system presents a BER performance of 3.1×10^{-3} without TE and of 6.8×10^{-4} after the TE routine, for a total Δ BER of 6.9 dB. This value represents the numerical evaluation of the BER improvement in terms of order of magnitude. Since one order of magnitude would correspond to 10 dB, the results obtained confirm an improvement greater than a half order of magnitude. For the experimental validation we also obtain an improvement of almost a half order of magnitude for all the cases considered. The performance improvement is also reported in terms of the Q factor.

TABLE I
SUMMARY OF TRANSMISSION RESULTS

| | Distance [km] | Increment Tolerance [dB] | Window [dB] | Δ BER [dB] | Q [dB] |
|---------------------------|---------------|--------------------------|-------------|-------------------|----------|
| Numerical single channel | 1000 | 2.5 | 5 | 5.1 | 0.75 |
| | 1500 | 3 | 6 | 6.8 | 1.36 |
| | 2000 | 2 | 4 | 5.2 | 1.30 |
| Experiment single channel | 240 | 3 | 6 | 4.6 | 0.75 |
| | 400 | 3 | 6 | 4.5 | 0.81 |
| | 640 | 3 | 6 | 5.2 | 1.01 |
| Experiment 100 GHz | 240 | 3 | 6 | 5.4 | 0.97 |
| | 400 | 3 | 6 | 4.7 | 0.97 |
| | 640 | 3 | 6 | 4.6 | 1.17 |

VII. CONCLUSION

We have reported the impact of the TE structure for mitigation of transmission impairments in a coherently detected PDM 16-QAM system. A CC has been employed at the transmitter side, while at the receiver the investigated TE is based on a NLMS as equalizer and on a SOVA as a decoder. We observe from our studies that TE is effective in mitigating fiber transmission impairments in a single channel PDM 16-QAM. We have accomplished up to 3 dB of increment in power tolerance and about a half order of magnitude BER gain for both unmanaged and managed transmission links. The first scenario has been evaluated by numerical investigations, the latter by experimental validation. The use of a TE routine can therefore also improve the maximum total and span length; 500 km longer transmission has been obtained in the numerical validation case. On the other hand, the benefit of this method can be addressed to relax the optical component, such as the laser linewidth; evaluation of the effect of the transmitter and receiver lasers' linewidth has been realized for a 1000 km unmanaged SSMF transmission realized by numerical validation. Additionally our proposed solution is proven to be effective in the transmission scenario where performance and reach are severely distorted by cross non-linear impairments due to the interactions with the copropagating ASK channels in a 100 GHz spectral grid. An increment in system tolerance of 3 dB is also reported in this case. Both the CC and equalizer in the TE loop contribute to the achieved improvements.

The results show the potential of the proposed TE routine for promising high-speed, high-capacity optical networking, such as PDM 16-QAM, over unmanaged and managed systems based on SSMF. Further improvement and some future research directions of the results could be (i) the use of gray mapping, (ii) the use of more powerful codes, and (iii) concatenation of the CC, and therefore of the TE scheme, with high-rate block codes.

APPENDIX A

In this appendix we show that the nongray mapping results in a specific calculation of the LLR values. In Fig. 9 two different mappings are shown: on the left side the gray mapping, and on the right side the nongray 16-QAM mapping resulting from the typical setup configuration of optical systems based on binary electronics. In Fig. 9 the value of the first two bits according to the region they belong to is also shown, for both mappings. As we can see, in the gray mapping design, if we move from left to right, only one bit of the two is changed every time we pass from one region to another. On the other side, in the nongray mapping, this feature is not present. We can notice that moving from region 2 to region 3 requires changing both bits at the same time. This fact also influences the LLR calculation.

The LLR calculation is realized for all four bits that constitute the 16-QAM signal and is based on the formulation reported in [24]. We indicate the four bits as $b_{Re,k} b_{Re,k} b_{Im,k} b_{Im,k}$ and $k = 0, 1$. The first two bits are

| Gray mapping | | | | Non-Gray mapping | | | |
|--------------|---------|---------|---------|------------------|---------|---------|---------|
| 0010 | 0110 | 1110 | 1010 | 0011 | 0111 | 1011 | 1111 |
| 0011 | 0111 | 1111 | 1011 | 0010 | 0110 | 1010 | 1110 |
| 0001 | 0101 | 1101 | 1001 | 0001 | 0101 | 1001 | 1101 |
| 0000 | 0100 | 1100 | 1000 | 0000 | 0100 | 1000 | 1100 |
| $b_0=0$ | $b_0=0$ | $b_0=1$ | $b_0=1$ | $b_0=0$ | $b_0=0$ | $b_0=1$ | $b_0=1$ |
| ① | ② | ③ | ④ | ① | ② | ③ | ④ |
| $b_1=0$ | $b_1=1$ | $b_1=1$ | $b_1=0$ | $b_1=0$ | $b_1=1$ | $b_1=0$ | $b_1=1$ |
| ① | ② | ③ | ④ | ① | ② | ③ | ④ |

Fig. 9. Gray, left side, and nongray, right side, mapping employed in the system.

derived from the real part of the signal, while the last two are from the imaginary part of the signal. The idea is demapping the received signal into soft bits that have the same sign as provided by a hard detector and whose absolute value represents the reliability of the decision. The optimum hard decision on bit $b_{Re,k}$ is given by the rule

$$\hat{b}_{Re,k} = \beta \quad \text{if } P[b_{Re,k} = \beta|r] > P[b_{Re,k} = (1 - \beta)|r], \quad \beta = 0, 1, \quad (\text{A1})$$

where r represents the received signal

$$r = G_{ch} \cdot a + w, \quad (\text{A2})$$

where G_{ch} is the channel frequency response and w is the complex additive white Gaussian noise (AWGN). If we set $\beta = 1$, we can rewrite Eq. (A1) as

$$\hat{b}_{Re,k} = 1, \quad \text{if } \log \frac{P(r|b_{Re,k} = 1)}{P(r|b_{Re,k} = 0)} > 0. \quad (\text{A3})$$

When we consider $k = 0$ we obtain

$$\frac{P(r|b_{Re,0} = 1)}{P(r|b_{Re,0} = 0)} = \frac{e^{-\frac{(\gamma_{Re}-1)^2}{2\sigma^2}} + e^{-\frac{(\gamma_{Re}-3)^2}{2\sigma^2}}}{e^{-\frac{(\gamma_{Re}+1)^2}{2\sigma^2}} + e^{-\frac{(\gamma_{Re}+3)^2}{2\sigma^2}}}. \quad (\text{A4})$$

The formulation in Eq. (A4) has been obtained considering that when $b_{Re,0} = 0$ the real part of the 16-QAM can only assume negative values, -3 or -1 , and when $b_{Re,0} = 1$ the real part of the 16-QAM can only assume positive values, $+1$ or $+3$. Therefore the LLR formulation for $b_{Re,0}$ is the same as reported in [24]

$$\text{LLR}_{\text{Re},0} = \begin{cases} \frac{4}{\sigma^2}(\gamma_{\text{Re}}[i] + 1), & \gamma_{\text{Re}}[i] < -2, & \text{region 1} \\ \frac{2}{\sigma^2}\gamma_{\text{Re}}[i], & |\gamma_{\text{Re}}[i]| \leq 2, & \text{regions 2 \& 3} \\ \frac{4}{\sigma^2}(\gamma_{\text{Re}}[i] - 1), & \gamma_{\text{Re}}[i] > +2, & \text{region 4} \end{cases} \quad (\text{A5})$$

Similarly to what is obtained for $b_{\text{Re},0}$, we can obtain the formulations for $b_{\text{Re},1}$:

$$\frac{P(r|b_{\text{Re},1} = 1)}{P(r|b_{\text{Re},1} = 0)} = \frac{e^{-\frac{(\gamma_{\text{Re}}-3)^2}{2\sigma^2}} + e^{-\frac{(\gamma_{\text{Re}}+1)^2}{2\sigma^2}}}{e^{-\frac{(\gamma_{\text{Re}}-1)^2}{2\sigma^2}} + e^{-\frac{(\gamma_{\text{Re}}+3)^2}{2\sigma^2}}}. \quad (\text{A6})$$

The LLR formulation in Eq. (A6) has been obtained considering that when $b_{\text{Re},1} = 0$ the real part of the 16-QAM can only assume values -3 or $+1$, and when $b_{\text{Re},1} = 1$ the real part of the 16-QAM can only assume values -1 or $+3$.

We now consider $b_{\text{Re},1}$. In region 2, when $-2 \leq \gamma_{\text{Re}} < 0$, we can assume that the relative contribution by constellation point $+3$ in the numerator [Eq. (A8)] can be ignored. Therefore the likelihood ratio reduces to

$$\frac{P(r|b_{\text{Re},1} = 1)}{P(r|b_{\text{Re},1} = 0)} \approx \frac{e^{-\frac{(\gamma_{\text{Re}}+1)^2}{2\sigma^2}}}{e^{-\frac{(\gamma_{\text{Re}}+3)^2}{2\sigma^2}} + e^{-\frac{(\gamma_{\text{Re}}-1)^2}{2\sigma^2}}}. \quad (\text{A7})$$

Expressing Eq. (A7) in logarithm form and considering negligible the added term $e^{(-8)/2\sigma^2}$, we obtain the LLR formula for $b_{\text{Re},1}$ in region 2 as

$$\text{LLR}(b_{\text{Re},1})_{\text{reg 2}} = \frac{2}{\sigma^2}(-\gamma_{\text{Re}}). \quad (\text{A8})$$

Considering all four regions for $b_{\text{Re},0}$ and $b_{\text{Re},1}$ we obtain the LLR formulas summarized in Table II.

The LLR formulas calculation for $b_{\text{Im},0}$ and $b_{\text{Im},1}$ follows the same rules as for $b_{\text{Re},0}$ and $b_{\text{Re},1}$. The results obtained are therefore the same, but on the imaginary part of the signal. We assume that all the clusters have the same variance and we therefore remove the factor $2/\sigma^2$ from all the LLR formulas. A study on the different variances of the 16 clusters can lead to a more precise calculation of the LLR and therefore to better performance.

The remapping block, placed after the SOVA decoder in the TE routine, works with the inverse formula reported in Table II. The four LLR values are then used to reconstruct the real and imaginary signals. It should be noted that only

one of the LLR values between $b_{\text{Re},0}$ and $b_{\text{Re},1}$ is necessary to reconstruct the real part, and only one between $b_{\text{Im},0}$ and $b_{\text{Im},1}$ to reconstruct the imaginary part. Due to this fact and to the mapping scheme, the reconstruction process may present jumps beyond the nearest cluster of the constellation. For example, let us consider the complex signal $+1.3 + 1.3j$. It will be demapped into 1010, and the LLRs are calculated with the formulas presented. Let us now assume that we have a decoder/re-encoder error, and the new bits are 0010. In this case we can notice that the corrections of the error forced us to move from region 3 to region 1 for the real part of the signal, and therefore not to the nearest clusters.

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TABLE II
LLR FORMULAS FOR $b_{\text{Re},0}$ AND $b_{\text{Re},1}$

| | | LLR($b_{\text{Re},0}$) | LLR($b_{\text{Re},1}$) |
|----------|-----------------|--|--|
| Region 1 | $y < -2$ | $(4/\sigma^2)(\gamma_{\text{Re}} + 1)$ | $(2/\sigma^2)(\gamma_{\text{Re}} + 2)$ |
| Region 2 | $-2 \leq y < 0$ | $(2/\sigma^2)\gamma_{\text{Re}}$ | $(2/\sigma^2)(-\gamma_{\text{Re}})$ |
| Region 3 | $0 \leq y < +2$ | $(2/\sigma^2)\gamma_{\text{Re}}$ | $(2/\sigma^2)(-\gamma_{\text{Re}})$ |
| Region 4 | $y \geq +2$ | $(4/\sigma^2)(\gamma_{\text{Re}} - 1)$ | $(2/\sigma^2)(\gamma_{\text{Re}} - 2)$ |

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